

## Dynamics test

AT Dynamics (09)

**Directions:** Solve the following problems, showing all work and circling your answer. Each is worth 5 points. Also, check the data below and make any needed changes.

- 1) A crane is being used to lift a 2000 kg box. The maximum tension the crane cable can support is 22,000 N.
- a. Determine the weight of the box.

$$w = mg = (2000 \text{ kg})(9.8 \text{ m/s}^2) = 19600 \text{ N}$$

- b. Determine the greatest acceleration the crane can impart onto the box.



$$\Sigma F_y = T - w = ma$$

$$\frac{T - w}{m} = a$$

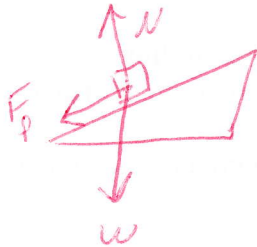
$$\frac{T - mg}{m} = a = \frac{(22,000 \text{ N}) - (2,000 \text{ kg})(9.8 \text{ m/s}^2)}{(2,000 \text{ kg})}$$

$$1.2 \text{ m/s}^2$$

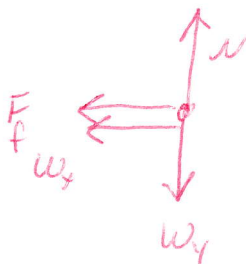
30  
25  
20  
15  
10  
5  
0

- 2) You are driving your pick-up truck at 22 m/s. In the bed of the pick-up, you have a large cardboard box. Determine your shortest possible stopping distance without the box sliding if you are going uphill at a 12 degree angle. The truck has a mass of 2,000 kg and the box has a mass of 150kg. You are listening to Led Zeppelin at the time you are trying to stop.

a. Draw a body diagram of this situation.



b. Draw a free body diagram of this situation



c. Solve the problem as stated above.

$$\begin{aligned} \Sigma F_x = F_f - W_x &= ma & \Sigma F_y = N - W_y &= 0 \\ & & N - W \cos \theta &= 0 \\ & & N &= mg \cos \theta \\ \mu N - W \sin \theta &= ma \\ \mu mg \cos \theta - mg \sin \theta &= ma \\ \mu g \cos \theta - g \sin \theta &= a \\ g[\mu \cos \theta - \sin \theta] &= a \end{aligned}$$

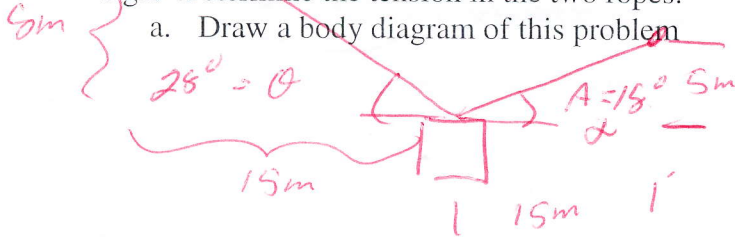
Bonus - Road Level?

$$\begin{aligned} v_0 &= 22 \text{ m/s} \\ a &= g[\mu \cos \theta + \sin \theta] \\ v &= \text{zero} \\ x &= ? \end{aligned}$$

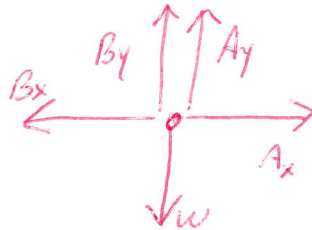
$$\begin{aligned} v^2 &= v_0^2 + 2ax \\ \frac{v_0^2}{2g(\mu \cos \theta + \sin \theta)} &= x = \frac{(22 \text{ m/s})^2}{2(9.8 \frac{\text{m}}{\text{s}^2})[0.4 \cos(12) + \sin(12)]} \end{aligned}$$

$$x = 41 \text{ m}$$

- 3) A 12kg sign is supported over a road by two ropes. Rope "A" is connected to the sign, and then is connected to a tall building that is 15 m away from the sign, and 5 m above the sign. Rope "B" is connected to the other side of the sign and is connected to a building that is also 15 m away from the sign, and 8 m above the sign. Determine the tension in the two ropes.



- b. Draw a free body diagram of this problem.



- c. Solve for the tension in rope "A"

$$\sum F_x = A_x - B_x = 0$$

$$A_x = B_x$$

$$A \cos \alpha = B \cos \theta$$

$$\frac{A \cos \alpha}{\cos \theta} = B$$

$$\frac{A \cos \alpha}{\cos \theta}$$

$$\sum F_y = A_y + B_y - W = 0$$

$$A \sin \alpha + B \sin \theta = W$$

$$A \sin \alpha + \frac{A \cos \alpha \sin \theta}{\cos \theta} = mg$$

$$A \left[ \sin \alpha + \frac{\cos \alpha \sin \theta}{\cos \theta} \right] = mg$$

$$A = \frac{mg}{\left[ \sin \alpha + \frac{\cos \alpha \sin \theta}{\cos \theta} \right]} = \frac{(12 \text{ kg})(9.8 \text{ m/s}^2)}{\left[ \sin 15^\circ + \frac{\cos 15^\circ (\sin 28^\circ)}{\cos 28^\circ} \right]} = 144 \text{ N} = A$$

- d. Solve for the tension in rope "B"

$$B \cos \theta = A \cos \alpha$$

$$B = \frac{A \cos \alpha}{\cos \theta} = \frac{(144 \text{ N}) \cos 15^\circ}{\cos 28^\circ} = 155 \text{ N} = B$$

4) Determine the weight of a 15 kg object.

$$W = mg = (15 \text{ kg})(9.8 \text{ m/s}^2) = 147 \text{ N}$$