

Thermal Physics

AT Thermal (11)

Solve the following problems showing ALL work and CIRCLING your answers. Each is worth 5 points. There is a table of information on the back of the test.

- 1) Determine the change in length of 30 miles of railroad track (steel) between a chilly winter day (0°C) and a warm summer day (32°C).

$$\Delta L = L_0 \alpha \Delta T$$

$$\Delta L = (30 \text{ mi}) (12 \times 10^{-6} / ^{\circ}\text{C}) (32^{\circ}\text{C})$$

$$\Delta L = .01152 \text{ mi} = 18.4 \text{ m}$$

- 2) A 300 Watt immersion heater is used to warm water. If the immersion heater is placed in a well-insulated cup with 0.5kg of water, how long will it take for the water to warm from room temperature (20°C) to the boiling point?

$$Q = mc\Delta T \quad (100^{\circ}\text{C} - 20^{\circ}\text{C})$$

$$Q = (.5 \text{ kg}) (4190 \text{ J/kg}^{\circ}\text{C}) (80^{\circ}\text{C})$$

$$Q = 167600 \text{ J}$$

$$(167600 \text{ J}) \left(\frac{1 \text{ s}}{300 \text{ J}} \right) = 558.7 \text{ s} = 9.3 \text{ min}$$

- 3) 3 kg of boiling water are poured into a 5 kg aluminum kettle at room temperature (20°C). Assume no thermal energy is lost; determine the temperature of the kettle and the water once it reaches thermal equilibrium.

$$Q_{\text{Water}} + Q_{\text{Al}} = 0$$

$$mC\Delta T + mC\Delta T = 0$$

$$m_C(T - T_0)_W + m_C(T - T_0)_A = 0$$

$$(3\text{kg})(4190\text{J/kg}\cdot^\circ\text{C})(T - 100^\circ\text{C}) + (5\text{kg})(900\text{J/kg}\cdot^\circ\text{C})(T - 20^\circ\text{C}) = 0$$

$$(12570\text{J/}^\circ\text{C})(T) - 1257000\text{J} + (4500\text{J/}^\circ\text{C})T - 90000\text{J} = 0$$

$$(12570\text{J/}^\circ\text{C})T + (4500\text{J/}^\circ\text{C})T = 1257000\text{J} + 90000\text{J}$$

$$(17070\text{J/}^\circ\text{C})T = \overset{1347000}{\cancel{2157000}}\text{J}$$

$$T = 78.9^\circ\text{C}$$

- 4) Determine the amount of ice (mass) that is needed to cool 5 kg of water at 20°C to water that is at 2°C. Assume no energy is lost to the surroundings.

$$\begin{array}{ccc} mL + mL\Delta T + mL\Delta T = 0 \\ \text{Ice} & \text{Water} & \text{Water} \\ & \text{That} & \\ & \text{Was} & \\ & \text{Ice} & \end{array}$$

$$m(3.34 \times 10^5 \text{ J/kg}) + m(4190 \text{ J/kg}^\circ\text{C})(2^\circ\text{C} - 10^\circ\text{C}) + (5 \text{ kg})(4190 \text{ J/kg}^\circ\text{C})(2 - 20^\circ\text{C}) = 0$$

$$m(342360 \text{ J/kg}) - 377100 \text{ J} = 0$$

$$m(342360 \text{ J/kg}) = 377100 \text{ J}$$

$$m = \frac{377100 \text{ J}}{342360 \text{ J/kg}}$$

$$m = 1.1 \text{ kg}$$

Thickness 2cm

- 5) A Styrofoam cooler has a surface area of 2 m^2 . Determine how long it will take for 2 kg of ice to melt if all of the energy is lost by conduction. Assume the air temperature outside the cooler remains constant at 20°C

$$\frac{Q}{t} = \frac{kA(\Delta T)}{L}$$

$$\frac{mL}{t} = \frac{kA(\Delta T)}{L_{\text{Thickness}}}$$

$$\frac{mL L_{\text{Thickness}}}{kA(\Delta T)} = t$$

$$\frac{(2 \text{ kg})(3.34 \times 10^5 \text{ J/kg})(.02 \text{ m})}{(.042 \text{ J/ms}^\circ\text{C})(2 \text{ m}^2)(20^\circ\text{C} - 0^\circ\text{C})} = t = 7952 \text{ s} = 132 \text{ min} = 2.2 \text{ hrs}$$

- 6) 2 kg of ice are placed in a black box with emissivity of 0.8. The box has a surface area of 2 m^2 . Determine how long it will take for the ice to melt if all of the energy exchange is only by radiation. The air outside the box is at 20°C .

$$20^\circ\text{C} = 293\text{K}$$

$$\frac{Q}{t}_{\text{Absorbed from Air}} - \frac{Q}{t}_{\text{Radiated}} = \frac{Q}{t}_{\text{net}}$$

$$\sigma \epsilon A T^4 - \sigma \epsilon A T^4 = \frac{Q}{t}_{\text{net}}$$

$$\sigma \epsilon A (T_{\text{Air}}^4 - T_{\text{ice}}^4) = \frac{Q}{t}$$

$$(5.67 \times 10^{-8}) \frac{\text{W}}{\text{m}^2 \text{K}^4} (0.8) (2 \text{ m}^2) (293\text{K}^4 - 273\text{K}^4) = \frac{Q}{t}$$

$$\underline{164.7 \frac{\text{J}}{\text{s}} = \frac{Q}{t} \text{ Rate}}$$

$Q = mL \Rightarrow$ Energy To melt Ice

$$Q = (2 \text{ kg}) (3.34 \times 10^5 \text{ J/kg}) = \underline{668,000 \text{ J}}$$

$$(668,000 \text{ J}) \left(\frac{1}{164.7 \text{ J/s}} \right) = \underline{4055 \text{ s} = 67 \text{ min}}$$