

Work and Energy

AT work and energy (10)

Directions: Solve the following problems, showing all work and circling your answer.
Each is worth 5 points

- 1) A 1200 kg is cruising down the road at 15 m/s. Determine the work that must be done to stop the car?

$$KE = W = \frac{1}{2}mv^2 = \left(\frac{1}{2}\right)(1200\text{kg})(15\text{m/s})^2 =$$

$$135,000\text{J}$$

- 2) A 2 kg mass is moving at 5 m/s horizontally, and strikes a horizontally mounted spring that has a spring constant of 45 N/m. Determine how far the spring is compressed in the process of stopping the 2 kg mass.

$$KE = PE$$

$$\frac{1}{2}mv^2 = \frac{1}{2}kx^2$$

$$mv^2 = kx^2$$

$$\sqrt{\frac{mv^2}{k}} = x =$$

$$\sqrt{\frac{(2\text{kg})(5\text{m/s})^2}{(45\text{N/m})}} = 1.05\text{m}$$

- 3) Determine the power rating required of a motor that is powering a go-cart that has a total of resistive forces (air resistance, and other friction) of 1220 N when traveling at 12 m/s.

$$P = \frac{W}{t} = \frac{F \cdot d}{t} = F \cdot v = (1220 \text{ N})(12 \text{ m/s}) =$$

14,640 Watts

19.6 h.p.

- 4) A spring with a spring constant of 20 N/m is stretched 2 m (Wow!!! That's far!!). Determine the amount of work that is done.

$$W = \frac{1}{2} k x^2$$

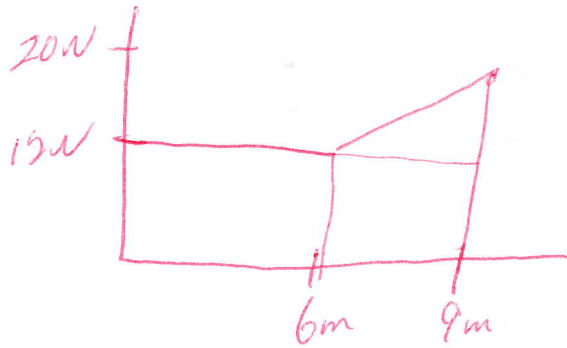
$$W = \left(\frac{1}{2}\right) (20 \text{ N/m}) (2 \text{ m})^2$$

$$W = 40 \text{ J}$$

- 5) A pulley arrangement is used to lift a 158 kg mass. A person pulls 5 meters of rope as the mass raises 0.5 meters. Determine the ideal mechanical advantage of this machine.

$$IMA = \frac{x_{in}}{x_{out}} = \frac{5m}{0.5m} = 10$$

- 6) A constant force of 12 N acts to move an object through a distance of 6 m. Once the object has moved through the 6 m, the force increases steadily until a force of 20 N is being applied. While the force was increasing, the object moved through an additional 3 m. Determine the work done while the object moved through the 9 m distance.



$$(12\text{N})(9\text{m}) = 108\text{J}$$

$$\left(\frac{1}{2}\right)(8\text{N})(3\text{m}) = 12\text{J}$$

$$120\text{J}$$

- 7) A 2 kg mass stretches a spring 12cm. How far will a 3.5 kg mass stretch the spring?

$$F_1 = kx_1$$

$$\frac{F}{x_1} = k$$

$$\frac{m_1 g}{x_1} = k$$

$$F_2 = kx_2$$

$$\frac{m_2 g}{x_2} = k$$

$$m_2 g = \frac{m_1 g}{x_1} x_2$$

$$\frac{m_2 g x_1}{m_1 g} = x_2$$

$$\frac{m_2 x_1}{m_1} = x_2 = \frac{(3.5 \text{ kg})(12 \text{ cm})}{2 \text{ kg}} = 21 \text{ cm}$$

- 8) Sledding down hills is really fun. On a really slippery, icy hill, you measure your speed at the bottom to be 12 m/s. How high was the hill?

$$PE = KE$$

$$mgh = \frac{1}{2}mv^2$$

$$2gh = v^2$$

$$h = \frac{v^2}{2g}$$

$$h = \frac{(12 \text{ m/s})^2}{2(9.8 \text{ m/s}^2)}$$

$$h = 7.35 \text{ m}$$